

# Test a perturbative QCD prediction with $e^+e^- \rightarrow D^{*+}D^{*-}$

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**Abstract:** The differential cross section for  $e^+e^- \rightarrow D^{*+}D^{*-}$  process was calculated in terms of the electromagnetic form factors of  $D^*$  meson. After putting in the ratios of form factors predicted by perturbative QCD (quantum chromodynamics), the angular distribution obtained was found to be inconsistent with experimental measurement at  $\sqrt{s}=10.58$  GeV.

**Key words:**  $D^*$  meson; electromagnetic form factor; perturbative QCD

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## 用 $e^+e^- \rightarrow D^{*+}D^{*-}$ 检验一个微扰 QCD 预言

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**摘要:** 计算了  $e^+e^- \rightarrow D^{*+}D^{*-}$  过程的微分截面, 以  $D^*$  介子的电磁形状因子表示. 代入微扰 QCD 预言的电磁形状因子比值, 得到的角分布与中心系能量为 10.58 GeV 的实验测量不一致.

**关键词:**  $D^*$  介子; 电磁形状因子; 微扰 QCD

### 0 Introduction

For hard exclusive processes, perturbative QCD predicts the following selection rule<sup>[1-2]</sup>:

$$\sum_{\text{initial}} \lambda_H = \sum_{\text{final}} \lambda_H,$$

i. e., total hadronic helicity is conserved. The equality is up to corrections of order  $M/Q$  or higher. This selection rule is implied in a formula for the asymptotic power behavior of any form factor<sup>[3]</sup>:

$$\langle p'\lambda' | J^\mu | p\lambda \rangle \sim \left( \frac{1}{Q} \right)^{(n_{\text{min}} + n'_{\text{min}} - 3) + |\lambda' - \lambda|}.$$

In particular, for processes  $e^+e^- \rightarrow \gamma^* \rightarrow hh'$ , the hadronic-helicity conservation rule is  $0 = \lambda + \lambda'$ . Angular momentum conservation requires  $|\lambda - \lambda'| \leq 1$ . Therefore for meson pairs  $\lambda = \lambda' = 0$ , and for baryon pairs  $\lambda = -\lambda' = \pm 1/2$ . Thus angular distributions are  $\sin^2\theta$  and  $1 + \cos^2\theta$  for meson pairs and baryon pairs, respectively. These predictions are nontrivial for vector mesons and for all baryons<sup>[1]</sup>.

Further, for spin-1 bound states, the dominance of helicity-conserving amplitudes implies that the charge, magnetic and quadrupole

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form factors have universal ratios, which will be shown in the next section.

Study of the process  $e^+e^- \rightarrow D^{*+}D^{*-}$  provides a chance to test this perturbative QCD prediction. It also allows investigation of electromagnetic form factors in the time-like region of momentum transfer.

## 1 Electromagnetic structure of spin-1 particle

For the matrix element of the electromagnetic current  $J^\mu$  of spin-1 system  $G_{\lambda\lambda'}^\mu = \langle p'\lambda' | J^\mu | p\lambda \rangle$ , where  $|p\lambda\rangle$  is eigenstate of momentum  $p$  and helicity  $\lambda$ , conventionally the most general form allowed by parity conservation and time reversal invariance can be written in terms of three Lorentz-invariant form factors<sup>[4-7]</sup>:

$$\begin{aligned} G^\mu(Q^2) = & -G_1(Q^2)\epsilon'^* \cdot \epsilon(p^\mu + p'^\mu) + \\ & G_2(Q^2)(\epsilon'^*{}^\mu \epsilon \cdot q - \epsilon''{}^\mu \epsilon'^* \cdot q) + \\ & G_3(Q^2)\frac{1}{2M^2}\epsilon \cdot q \epsilon'^* \cdot q(p^\mu + p'^\mu), \end{aligned}$$

where  $q = p' - p$  and  $Q^2 = |q^2|$ .  $\epsilon$  and  $\epsilon'$  are initial and final polarization vectors, respectively.  $M$  is the mass of the particle.

These form factors are related to the charge, magnetic and quadrupole form factors<sup>[6]</sup>:

$$G_C = G_1 + \frac{2}{3}\eta G_Q,$$

$$G_M = G_2,$$

$$G_Q = G_1 - G_2 + (1 + \eta)G_3,$$

where  $\eta = -q^2/(4M^2)$  is a kinematic factor. Their static limits are

$$eG_C(0) = e,$$

$$eG_M(0) = 2M\mu_1,$$

$$eG_Q(0) = M^2 Q_1$$

with  $\mu_1$  being the magnetic moment and  $Q_1$  the quadrupole moment.

By inverting the relationship between current matrix elements and form factors in the standard light-cone frame, and assuming that  $G_{00}^+$  matrix element is the dominant amplitude<sup>[8]</sup>, it is shown that the charge, magnetic, and quadrupole form factors have universal ratios<sup>[7]</sup>:

$$G_C : G_M : G_Q = \left[1 - \frac{2}{3}\eta\right] : 2 : -1.$$

These ratios hold for composite systems such as  $\rho$  meson or deuteron at large space-like or time-like momentum transfer, i. e.  $Q \gg \Lambda_{\text{QCD}}$ , up to corrections of order  $\Lambda_{\text{QCD}}/Q$  and  $\Lambda_{\text{QCD}}/M$ . It is argued that there should also be  $Q \gg \sqrt{2M\Lambda_{\text{QCD}}}$ <sup>[7]</sup>.

In addition, these ratios hold for  $W^\pm$  form factors at the tree level, which means that the ratios of form factors of bound states become identical to those of elementary particles at large momentum transfer.

## 2 $e^+e^- \rightarrow D^{*+}D^{*-}$ differential cross section

For  $e^+e^- \rightarrow \gamma^* \rightarrow D^{*+}D^{*-}$  process,  $D^*$  current matrix element is

$$\begin{aligned} G^\mu(q^2) = & -G_1(q^2)\epsilon'^* \cdot \epsilon^*(k'^\mu - k^\mu) + \\ & G_2(q^2)(\epsilon'^*{}^\mu \epsilon^* \cdot q - \epsilon^*{}^\mu \epsilon'^* \cdot q) + \\ & G_3(q^2)\frac{1}{2M^2}\epsilon^* \cdot q \epsilon'^* \cdot q(k'^\mu - k^\mu), \end{aligned}$$

where  $k$  and  $k'$  are momentum of the  $D^*$ 's, and now  $q = k + k' = \sqrt{s}$ .

The unpolarized differential cross section in the center-of-mass frame is calculated:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{8E_{\text{CM}}^2}(1 + 1/\eta)^{3/2}(C_1 + C_2 \cos^2 \theta),$$

$$C_{1,2} = \pm 3 |G_C|^2 - 2\eta |G_M|^2 \pm \frac{8}{3}\eta^2 |G_Q|^2.$$

The angular distribution of  $D^{*\pm}$  in CM frame is of the form  $1 + \beta \cos^2 \theta$ . At the energy of BELLE experiment,  $\sqrt{s} = 10.58$  GeV, and given the predicted ratios of form factors,

$$G_C : G_M : G_Q = \left[1 - \frac{2}{3}\eta\right] : 2 : -1, \beta = -0.60$$

is obtained.

It should be noted that although it was mentioned in Ref. [7] that for the time-like reaction  $\eta = s/(4M^2)$ , its definition, as we have observed, should be coherent in the space-like and time-like region,  $\eta = -q^2/(4M^2)$ , which is  $-s/(4M^2)$  in the time-like case.

### 3 Discussion

An experimental analysis at BELLE<sup>[9]</sup> gives  $\beta = 0.79_{-0.30}^{+0.34}$ , which is not in agreement with the perturbative QCD predictions: neither  $\beta = -1(\sin^2\theta)$  as a result of hadronic-helicity conversation, nor  $\beta = -0.60$  assuming the dominance of  $G_{00}^+$ .

BABAR Collaboration has presented an analysis of  $e^+e^- \rightarrow \rho^+\rho^-$  process<sup>[10]</sup> and also reported an inconsistency with the prediction of perturbative QCD with a significance of 3.1 standard deviations including systematic uncertainties.

A discussion about relations between the Breit frame and the light-front frame<sup>[11]</sup> has shown that the angular condition in light-front frame, which is derived from conservation of angular momentum in Breit frame, contradicts the hypothesis that the scale of the asymptotic power-law falloff of non-leading amplitudes is set by  $\Lambda_{\text{QCD}}$ . It is suggested that this scale would be of the order of the particle mass. As a consequence, next-to-leading corrections are non-negligible and the underlying assumption in Ref. [7] that  $G_{00}^+$  is dominant at large  $Q^2$  needs to be reconsidered.

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